

Optimal Signal Demixing

Applications for Energy Data

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October 2019



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- 2 Methodology: Signal Demixing
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Background: More Data, More Opportunities

- Increasing volume of photovoltaic (PV) system performance data creates opportunities for **monitoring system health** and **optimizing operations and maintenance (O&M) activities**.
- Digital O&M \$9b industry by 2024 (“The State of Digital O&M for the Solar Market”, *Greentech Media*, 10/10/19)
- However, classic approaches—waterfall analysis, performance index analysis—require
 - A significant amount of engineering time
 - Knowledge of PV system modeling science and best practices
 - Accurate system configuration information
 - Access to reliable irradiance and meteorological data

New Approaches are Needed

For these reasons, existing PV system performance engineering methods are focused on **utility scale power plants...**



Image credit: SunPower Corp.

...rather than the rapidly increasing number of **distributed rooftop systems.**



Image credit: Google Earth

Utility vs. Distributed

	Utility	Distributed
<i>Site model</i>	✓	✗
<i>Irradiance data</i>	✓	✗
<i>Meteorological data</i>	✓	✗
<i>People / PV system</i>	> 1	$\ll 1$

- New approaches needed to analyze and managed distributed PV
- How to extract insight into system health from only a power signal?

My Work So Far

- Proposed “PVInsight” to the U.S. Department of Energy Solar Energy Technologies Office (DOE SETO), which was successfully funded over two years (FY 2019-2020)
- One journal paper and one conference paper
 - B. Meyers, M. Deceglie, C. Deline, and D. Jordan, “Signal Processing on PV Time-Series Data: Robust Degradation Analysis without Physical Models,” *IEEE Journal of Photovoltaics* (accepted)
 - B. Meyers, M. Tabone, and E. C. Kara, “Statistical Clear Sky Fitting Algorithm,” *Proc. of IEEE 45th Photovolt. Spec. Conf.*, 2018.
- Three conference oral presentations
 - IEEE Photovoltaics Specialists Conference (2018, 2019)
 - NREL Reliability Workshop (2019)
- Two published open-source Python projects
 - solar-data-tools: <https://github.com/slacgismo/solar-data-tools>
 - StatisticalClearSky: <https://github.com/slacgismo/StatisticalClearSky>

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Background on Demixing Signals

$$y_t = (x_0)_t + \cdots + (x_K)_t \in \mathbf{R}^p$$

- Given y_t , estimate its **components** x_k
- Generally a highly underdetermined problem, but many useful approaches are possible
 - Filtering, PCA, ICA, NMF, basis pursuit
- Common themes:
 - Maximize independence or minimize correlation between components
 - Impose low-complexity constraints on components

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A Brief History

- Many names: blind source separation, disaggregation, decomposition, trend estimation...
- Fourier analysis formalized in late 18th to early 19th century (Fourier, Lagrange, Gauss...)
- PCA invented by Karl Pearson in 1901
- Trend-cycle decomposition and smoothing developed by Frederick Macaulay in the 1920s
- Sinc interpolation and low-pass filtering developed by Whittaker, Nyquist, Kotelnikov, Shannon in 1930s-1940s
- Colin Cherry defined and named the “cocktail party problem” in 1953
- ICA first developed by Jeanny Hérault and Bernard Ans in mid-1980s
 - Refined by Hyvärinen in 1999
- Basis pursuit proposed by Chen, Donoho, and Saunders in 2001
- Contextually supervised source separation proposed by Wytock and Kolter in 2013

Optimal Signal Demixing (OSD) Problem

$$\underset{\substack{x_0, \dots, x_K \\ \theta_0, \dots, \theta_K}}{\text{minimize}} \quad \sum_{k=0}^K \lambda_k \phi_k(x_k, \theta_k)$$

$$\text{subject to} \quad y_{i,t} = \sum_{k=0}^K (x_k)_{i,t} \quad \text{for } (i, t) \in \mathcal{K}$$

- Optimize over variables $x_k \in \mathbf{R}^{p \times T}$ and $\theta_k \in \mathbf{R}^{m_k}$ for $k = 0, \dots, K$
 - x_k are demixed components with x_0 being the noise term
 - θ_k are optional extra variables for parameterized models
- $y \in \mathbf{R}^{p \times T}$ is the observed signal (problem data) with set of known entries \mathcal{K}
- $\phi_k : \mathbf{R}^{p \times T} \rightarrow \mathbf{R} \cup \{\infty\}$ defines the **class** of component x_k
- $\lambda_k \geq 0$ trade off between importance of components' costs ($\lambda_0 = 1$ by convention)
- If all ϕ_k are convex in x_k and θ_k , it is a convex optimization problem

Component Classes

- Smaller $\phi_k(x) \rightarrow$ more plausible x_k is
- $\lambda_k \phi_k(x)$ can be interpreted as negative log-likelihood (assuming independence)
- Constraints can be incorporated in any class cost function by defining the function to be equal to infinity if constraints are violated
- For many useful choices of ϕ_k , OSD is a quadratic program (QP)

Noise Component Classes ($p = 1$)

<i>Class Description</i>	$\phi(x)$
Small, Gaussian	$\sum_{t=1}^T x_t^2$
Small, Laplacian (“spikey”)	$\sum_{t=1}^T x_t $
Small, skewed, set quantile τ	$\sum_{t=1}^T \left[\frac{1}{2} x_t + \left(\tau - \frac{1}{2} \right) x_t \right]$
Huber (thick-tailed Gaussian), set breakpoint a	$\sum_{t=1}^T \left[\begin{cases} \frac{1}{2} x_t^2 & x_t \leq a \\ a \left(x_t - \frac{a}{2} \right) & x_t > a \end{cases} \right]$

Structured Component Classes—Convex Examples ($p = 1$)

<i>Class Description</i>	$\phi(x)$
Smooth, slowly changing average	$\sum_{t=1}^{T-1} (x_{t+1} - x_t)^2$
Smooth, slowly changing slope	$\sum_{t=1}^{T-2} (x_{t+2} - 2x_{t+1} + x_t)^2$
Piecewise constant (heuristic)	$\sum_{t=1}^{T-1} x_{t+1} - x_t $
Piecewise linear (heuristic)	$\sum_{t=1}^{T-2} x_{t+2} - 2x_{t+1} + x_t $
Periodic, period q	$x_{t+q} = x_t$ for $t = 1, \dots, T - q$
Monotonically increasing	$x_{t+1} \geq x_t$ for $t = 1, \dots, T - 1$
Autoregressive, known coefficients α_i	$x_t = \alpha_1 x_{t-1} + \dots + \alpha_r x_{t-r}$ for $t = r + 1, \dots, T$
Linear model, new parameter θ	$x = A\theta$

Structured Component Classes—Non-Convex Examples ($p = 1$)

<i>Class Description</i>	$\phi(x)$
Piecewise constant (exact)	$\sum_{t=1}^{T-1} \mathbf{1}(x_{t+1} - x_t \neq 0)$
Piecewise linear (exact)	$\sum_{t=1}^{T-2} \mathbf{1}(x_{t+2} - 2x_{t+1} + x_t \neq 0)$
Autoregressive, unknown coefficients θ_i	$x_t = \theta_1 x_{t-1} + \dots + \theta_r x_{t-r}$ for $t = r + 1, \dots, T$
Discrete feasible values in set \mathcal{F}	$x_t \in \mathcal{F}$ for $t = 1, \dots, T$

Classic Examples of Filtering and Smoothing ($K = 1$)

- Hodrick-Prescott filtering¹
 - $\phi_0(x) = \sum_{t=1}^T x_t^2$
 - $\phi_1(x) = \sum_{t=1}^{T-2} (x_{t+2} - 2x_{t+1} + x_t)^2$
- Total variation denoising²
 - $\phi_0(x) = \sum_{t=1}^T x_t^2$
 - $\phi_1(x) = \sum_{t=1}^{T-1} |x_{t+1} - x_t|$
- Quantile smoothing³ (set quantile $0 < \tau < 1$)
 - $\phi_0(x) = \sum_{t=1}^T \left[\frac{1}{2} |x_t| + \left(\tau - \frac{1}{2} \right) x_t \right]$
 - $\phi_1(x) = \sum_{t=1}^{T-2} (x_{t+2} - 2x_{t+1} + x_t)^2$

¹C. E. V. Leser, "A Simple Method of Trend Construction," 1961.

²L. I. Rudin, S. Osher, and E. Fatemi, "Nonlinear total variation based noise removal algorithms," 1992.

³K. Abberger, "Quantile smoothing in financial time series," 1997.

Missing Data: Imputation and Validation

- Problem data $y \in \mathbf{R}^{p \times T}$ may have missing entries (?, NaN, etc.)
- $(i, t) \in \mathcal{K}$ are the known entries of y
- Imputation:
 - Solve OSD problem to estimate x_0, \dots, x_K
 - For $(i, t) \notin \mathcal{K}$, we guess $\hat{y}_{i,t} = (x_0)_{i,t} + \dots + (x_K)_{i,t}$
- Validation
 - Hold out some entries of y to make set \mathcal{K}' , and then compare with imputed value
 - Measure: $\sum_{(i,t) \in \mathcal{K}'} \phi_0(y_{i,t} - \hat{y}_{i,t})$

Convex Heuristics for Non-convex Cases

- Many useful ϕ_k are convex
- We can evaluate non-convex ϕ_k , but typically can't solve exactly
- ℓ_1 -norm approximation for cardinality minimization problems⁴
 - All total-variation type problems: edge detection, piecewise constant functions, piecewise linear functions, lasso regression
 - Compatible with polishing, iterative reweighting, and other heuristics for improving sparsity
- ADMM for mixed-integer constraints⁵
- Alternating convex optimization for biconvex ϕ_k 's

⁴Candès, et al., "Enhancing sparsity by reweighted L1 minimization," 2008.

⁵Takapoui, et al., "A simple effective heuristic for embedded mixed-integer quadratic programming," 2017.

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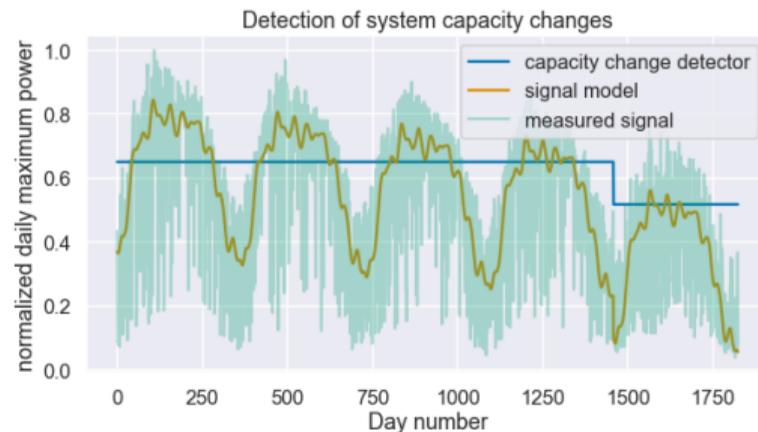
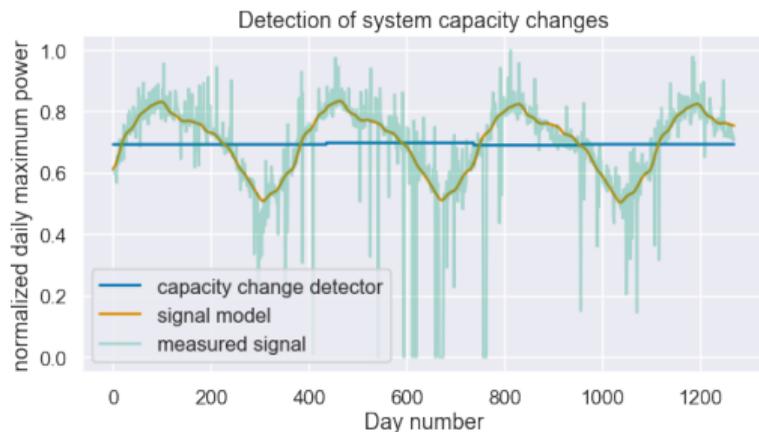
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System Capacity Change Detection

Problem: Detect equipment failure as a step-change in apparent PV system capacity

Component	Class	$\phi(x, \theta)$	λ
x_0	small, Laplacian	$\sum_{t=1}^T x_t $	1
x_1	smooth and 365-day periodic with linear offset	$\begin{cases} \sum_{t=1}^{T-2} (x_{t+2} - 2x_{t+1} + x_t)^2 + \theta^2 & x_{t+365} - x_t = \theta \\ \infty & x_{t+365} - x_t \neq \theta \end{cases}$	15
x_2	iteratively weighted ($w_t^{(j)}$) piecewise constant	$\sum_{t=1}^{T-1} w_t^{(j)} (x_{t+1} - x_t) $	100

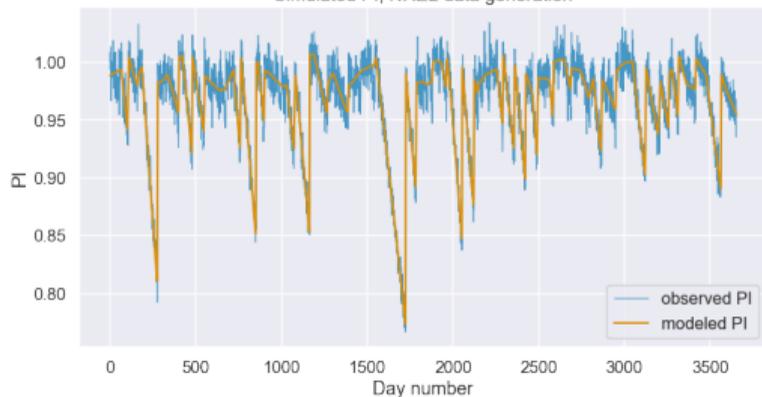


Soiling Analysis

Problem: Estimate soiling rates and energy loss from system performance index (PI)

Component	Class	$\phi(x, \theta)$	λ
x_0	small, Gaussian	$\sum_{t=1}^T x_t^2$	1
x_1	smooth and 365-day periodic	$\left\{ \begin{array}{l} \sum_{t=1}^{T-2} (x_{t+2} - 2x_{t+1} + x_t)^2 \\ \infty \end{array} \right. \begin{array}{l} x_{t+365} = x_t \\ x_{t+365} \neq x_t \end{array}$	10
x_2	iteratively weighted ($w_t^{(j)}$) piecewise linear	$\sum_{t=1}^{T-2} w_t^{(j)} (x_{t+2} - 2x_{t+1} + x_t) $	0.1

Simulated PI, NREL data generation



Hidden soiling signal, estimated versus groundtruth

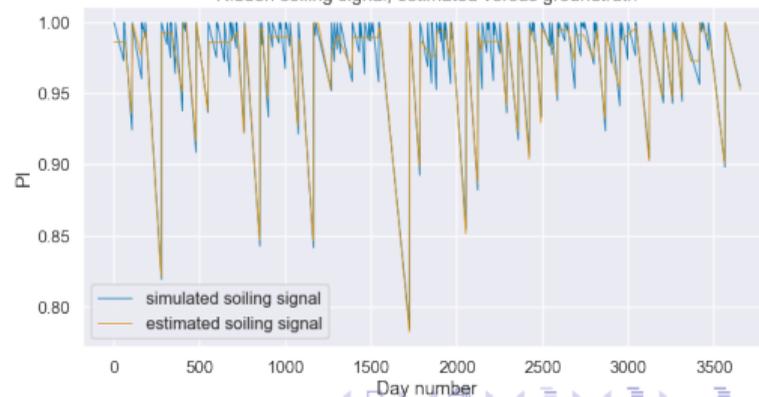


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Next Steps

- Continued literature review to establish connections with previous work
- Manuscript on proposed framework
- Python software package implementing framework, to be referenced in manuscript
- Continued application of methods to energy analysis problems
- Apply to forecasting and MPC problems

Appendix A: Additional background and papers on signal demixing

Background on Signal Separation

- The separation of a set of components from a set of mixed signals
- Colin Cherry defined and named the “cocktail party problem” in 1953⁶
- Generally a highly underdetermined problem, but many useful approaches are possible
- Problems are generally categorized by
 - The number of observed channels (single-channel or multi-channel)
 - The mixture process (linear instantaneous, delayed, convolutive, or non-linear)
- Common themes
 - Look for components that are maximally independent or minimally correlated
 - Principle component analysis, independent component analysis
 - Impose some kind of low-complexity constraint on components
 - Non-negative matrix factorization, basis pursuit, filtering methods

⁶E. C. Cherry, “Some Experiments on the Recognition of Speech, with One and with Two Ears,” *J. Acoust. Soc. Am.*, vol. 25, no. 5, pp. 975–979, Sep. 1953.

Background: Independent Component Analysis

- First proposed by Jeanny Héroult and Bernard Ans in around 1982–1984 (in French)
- Refined and clarified by Pierre Comon in 1994⁷
- Fast and efficient algorithm proposed by Anthony Bell and Terry Sejnowski in 1995⁸
- Modern interpretation is based on maximum likelihood estimation, in which we assume that sources are independent and non-Gaussian (typically logistic)
- Classically, ICA solves multi-channel, linear instantaneous problems, but other extensions have been proposed
- More recently single channel ICA has been explored, with mixed results⁹

⁷P. Comon, "Independent component analysis, A new concept?," *Signal Processing*, vol. 36, no. 3, pp. 287–314, 1994.

⁸A. J. Bell and T. J. Sejnowski, "An Information-Maximization Approach to Blind Separation and Blind Deconvolution," *Neural Comput.*, vol. 7, no. 6, pp. 1129–1159, 1995.

⁹M. E. Davies and C. J. James, "Source separation using single channel ICA," *Signal Processing*, vol. 87, no. 8, pp. 1819–1832, 2007.

Background: Dictionaries and Basis Pursuit

- Building upon classic representation of periodic signals as collection of sinusoids, many alternate **dictionaries** of parameterized waveforms have been proposed
 - Wavelets, Gabor dictionaries, Cosine Packets, Chirplets, and many more
- 1988: Ingrid Daubechies proposed the **Method of Frames** for finding decompositions of signals into both time and frequency¹⁰
- 2001: Chen, Donoho, and Saunders proposed **Basis Pursuit** for decomposing a signal into an optimal superposition of dictionary elements¹¹
- Chen et al. used convex optimization to find sparse signal representation, even with overcomplete dictionaries

¹⁰I. Daubechies, "Time-frequency localization operators: a geometric phase space approach," *IEEE Trans. Inf. Theory*, vol. 34, no. 4, pp. 605–612, Jul. 1988.

¹¹S. S. Chen, D. L. Donoho, and M. A. Saunders, "Atomic Decomposition by Basis Pursuit," *SIAM Rev.*, vol. 43, no. 1, pp. 129–159, Jan. 2001.

Appendix B: Additional examples

Classic Examples of Fitting and Smoothing ($k = 1$)

- Hodrick-Prescott filtering

- $\phi_0(x_0) = \|x_0\|_2^2$
- $\phi_1(x_1) = \|\Delta^2 x_1\|_2^2$

- Quantile smoothing

- $\phi_0(x_0) = \tau \mathbf{1}^T (x_0)_+ + (\mathbf{1} - \tau)^T (x_0)_-$
- $\phi_1(x_1) = \|\Delta^2 x_1\|_2^2$

- ℓ_1 trend filtering

- $\phi_0(x_0) = \|x_0\|_2^2$
- $\phi_1(x_1) = \|\Delta^2 x_1\|_1$

- Total variation filtering

- $\phi_0(x_0) = \|x_0\|_2^2$
- $\phi_1(x_1) = \|\Delta x_1\|_1$

- Autoregressive model, order r

- $\phi_0(x_0) = \|x_0\|_2^2$
- $\phi_1(x_1, \theta) = \begin{cases} 0 & (x_1)_t = \sum_{j=1}^r \theta_j (x_1)_{t-j} + \theta_0 \forall t \\ \infty & \text{otherwise} \end{cases}$

- Linear regression to time

- $\phi_0(x_0) = \|x_0\|_2^2$
- $\phi_1(x_1, \theta) = \begin{cases} 0 & (x_1)_t = \theta_1 t + \theta_0 \forall t \\ \infty & \text{otherwise} \end{cases}$

- Robust regression (B&V¹² example 6.2)

- $\phi_0(x_0) = \sum_{t=1}^n \text{huber}((x_0)_t)$
- $\phi_1(x_1, \theta) = \begin{cases} 0 & (x_1)_t = \theta_1 t + \theta_0 \forall t \\ \infty & \text{otherwise} \end{cases}$

¹²S. Boyd and L. Vandenberghe, *Convex Optimization*, Cambridge, U.K.: Cambridge Univ. Press, 2004